## Design of Flyer-Plate-Driven, Compressible-Turbulent-Mix Experiments

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Supernova
Simulation


Omega Laser Experiment


Z Flyer
Experiment

## Z has opened up new experimental possibilities



Shown above are pictures of the Z-pinch: (left) prior to firing (right) during firing

By imploding hundreds of wires,
Z can make MJ of X-rays

When the wires collide they produce up to
2 Mega-Joules of $x$-rays



# What matters here: Z can use J X B forces to launch Al flyer plates at > 20 km/s 



Photo: www.spacedaily.com/news/milspace-tech-01a.html

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# Flyer-plate mix experiments differ from flyer-plate EOS experiments 

- EOS experiments
- Need rock-steady shock
- Experiment ends when shock exits material
- Mix experiments
- Experiment begins when interface of interest is shocked
- May not want steady shock
- Even steady shock need not meet EOS constraints


## Basic geometry for flyer plate experiments



In the following:
Analytic results use $\gamma$-law gas, strong shock equations
Simulations used the HYADES Lagrangian hydrocode with SESAME EOS

## Basic relationships <br> for strong shocks in this system

In lab frame:
$u_{c s}=\frac{1}{1+\sqrt{\rho_{4} / \rho_{1}}} u_{F}$
$u_{R S}=\left(1-\frac{\gamma-1}{2} \sqrt{\frac{\rho_{4}}{\rho_{1}}}\right) \frac{u_{F}}{1+\sqrt{\rho_{4} / \rho_{1}}}$
$u_{F S}=\frac{\gamma+1}{2} \frac{u_{F}}{1+\sqrt{\rho_{4} / \rho_{1}}}$

In flyer frame:

$$
u_{R S}^{\prime \prime}=\frac{-\sqrt{\rho_{4} / \rho_{1}}}{1+\sqrt{\rho_{4} / \rho_{1}}} \frac{\gamma+1}{2} u_{F}
$$

Sound speeds:

$$
\begin{gathered}
c_{3}=\sqrt{\frac{\gamma(\gamma-1)}{2}} u_{C S}=\sqrt{\frac{\gamma(\gamma-1)}{2}} \frac{u_{F}}{1+\sqrt{\rho_{4} / \rho_{1}}} \\
c_{2}=\sqrt{\frac{\gamma(\gamma-1)}{2}}\left(u_{F}-u_{C S}\right)=\sqrt{\frac{\gamma(\gamma-1)}{2}} \frac{\sqrt{\rho_{4} / \rho_{1}}}{1+\sqrt{\rho_{4} / \rho_{1}}} u_{F}
\end{gathered}
$$

## In mix experiments one will often not use an Aluminum impact layer




# At lower impact layer density, one can drive steady shocks over larger distances 



Time until the shock reaches the rear of the flyer plate

$$
t=\frac{D_{1}}{\left|u_{R S}^{\prime \prime}\right|}
$$

How far the shock goes into the impact layer

$$
D_{4}=u_{F S} t=\frac{u_{F S}}{\left|u_{R S}^{\prime \prime}\right|} D_{1}=\sqrt{\frac{\rho_{1}}{\rho_{4}}} D_{1}
$$

## For RT experiments, one creates a blast wave

M
$350 \mu \mathrm{~m}$ thick, $21 \mathrm{~km} / \mathrm{s}$ flyer


Goal: waste none of the deceleration

$$
\begin{gathered}
t_{4}=\frac{D_{4}}{u_{F S}}=\frac{D_{4}}{u_{F}} \frac{2\left(1+\sqrt{\rho_{4} / \rho_{1}}\right)}{\gamma+1} \\
t_{1}=\frac{D_{1}}{\left|u_{R S}^{\prime \prime}\right|}+\frac{\gamma-1}{\gamma+1} \frac{D_{1}}{c_{2}}+\frac{\gamma-1}{\gamma+1} \frac{D_{4}}{c_{3}} \\
\boldsymbol{t}_{4}=\boldsymbol{t}_{\mathbf{1}} \text { so }
\end{gathered}
$$

$$
\frac{D_{4}}{D_{1}}=\sqrt{\frac{\rho_{1}}{\rho_{4}}} \frac{(1+\sqrt{(\gamma-1) / 2 \gamma})}{(1-\sqrt{(\gamma-1) / 2 \gamma})}
$$

## The unstable interface moves several mm




## This graph shows the interface behavior

- The linear growth exponent is ~30 by $1.5 \mu \mathrm{sec}$



## Richtmyer-Meshkov experiments are harder

Goal: maximum steady post-shock motion of interface
Means: make rarefactions in flyer and impact layer meet at contact surface

$$
\begin{gathered}
t_{1}=\frac{D_{1}}{\left|u_{R S}^{\prime \prime}\right|}+\frac{\gamma-1}{\gamma+1} \frac{D_{1}}{c_{2}}=\frac{D_{1}}{u_{F}} \frac{\left(1+\sqrt{\rho_{4} / \rho_{1}}\right)}{\sqrt{\rho_{4} / \rho_{1}}}\left(\frac{2}{\gamma+1}+\sqrt{\frac{2}{\gamma(\gamma-1)}}\right) \\
t_{4}=\frac{D_{4}}{u_{F S}}+\frac{\gamma-1}{\gamma+1} \frac{D_{4}}{c_{3}}=\frac{D_{4}}{u_{F}}\left(1+\sqrt{\rho_{4} / \rho_{1}}\right)\left\{\frac{2}{\gamma+1}+\sqrt{\frac{2}{\gamma(\gamma-1)}}\right\} \\
\boldsymbol{t}_{4}=\boldsymbol{t}_{\mathbf{1}} \text { so } \\
D_{4} / D_{1}=\sqrt{\rho_{1} / \rho_{4}}
\end{gathered}
$$

## An example where the rarefactions meet

四

$350 \boldsymbol{\mu m}$ thick, 21 km/s flyer

## The unstable interface moves steadily for ~ 1 mm




## Conclusions

- This poster has described design approaches for flyerdriven RT and RM experiments on $\mathbf{Z}$
- The advent of the $\mathbf{Z}$ backlighter makes these timely
- Z should be able to accomplish very interesting compressible turbulent mix experiments
- Join us the February 23-25, 2002 for the
- 4th International Conference on High Energy Density Laboratory Astrophysics
- At the University of Michigan in Ann Arbor


