

---

---

# **ALE Simulations of Turbulent Rayleigh-Taylor Instability in 2-D and 3-D**

---

---



**S. V. Weber, G. Dimonte, and M. M. Marinak**  
**Lawrence Livermore National Laboratory**

**2001 International Workshop on the Physics  
of Compressible Turbulent Mixing  
Pasadena, CA  
December 10-14, 2001**

# We have simulated the “ $\alpha$ - group” turbulent Rayleigh-Taylor problem in 2-D and 3-D with the ALE code, Hydra

---

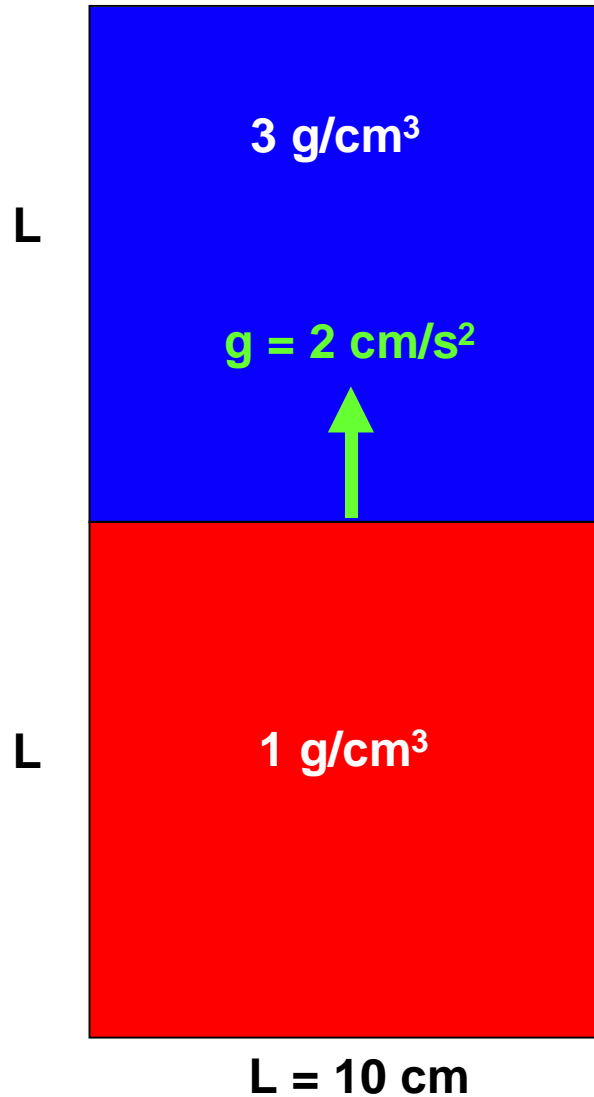


- Weakly compressible RT with a random initial surface spectrum restricted to short wavelength modes (4-8 zones/ $\lambda$ )
- Hydra is a 3-D parallel ALE code with interface reconstruction
- Zoning convergence is suspect
  - Simulated linear growth rates for the seed modes are as low as 15% of the correct classical value
  - In 3-D, modes with  $k$  aligned with the mesh grow faster than others
- We use a initial surface comprised of cosine modes to avoid aliasing due to reflection span-wise boundary conditions
- 2-D simulations show weak dependence on zoning up to  $1024 \times 2048$
- 3-D simulations with interface reconstruction predict  $\alpha_b \sim 0.03$ - $0.055$ ,  $\alpha_s \sim 0.06$
- Simulations without interface reconstruction show only slightly lower penetration but much more small-scale mixing

# Initial configuration & adiabatic equilibrium



256 x 256 x 512 zones

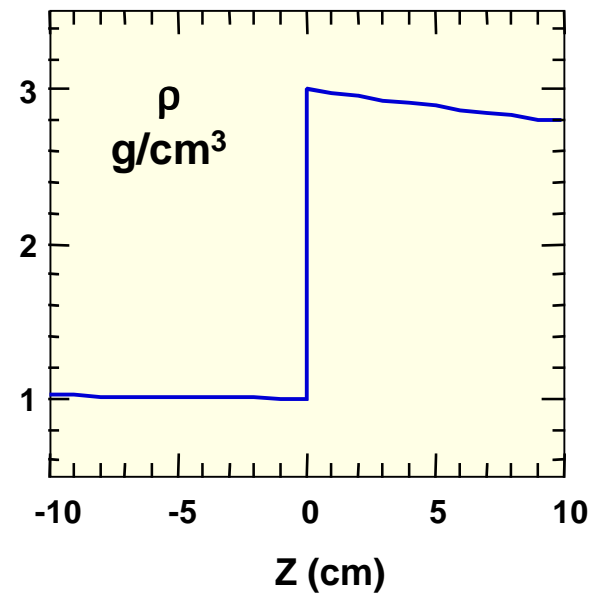


$$\frac{dP}{dz} = -\rho g$$

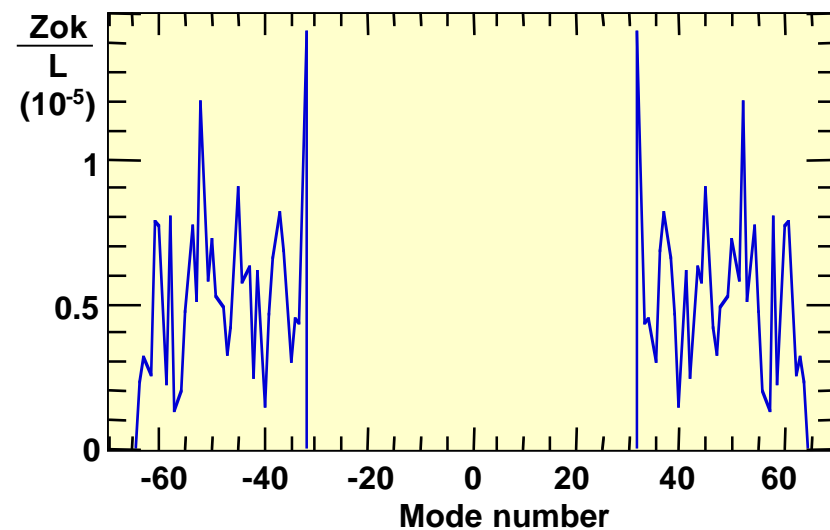
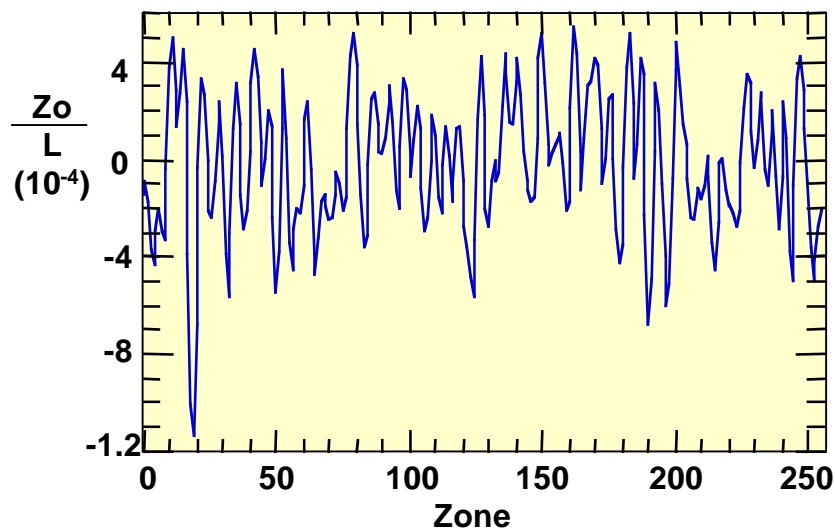
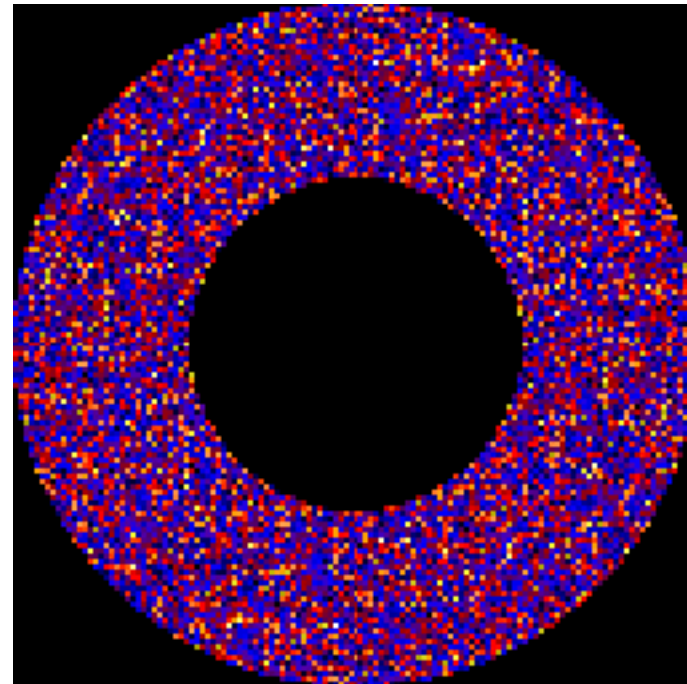
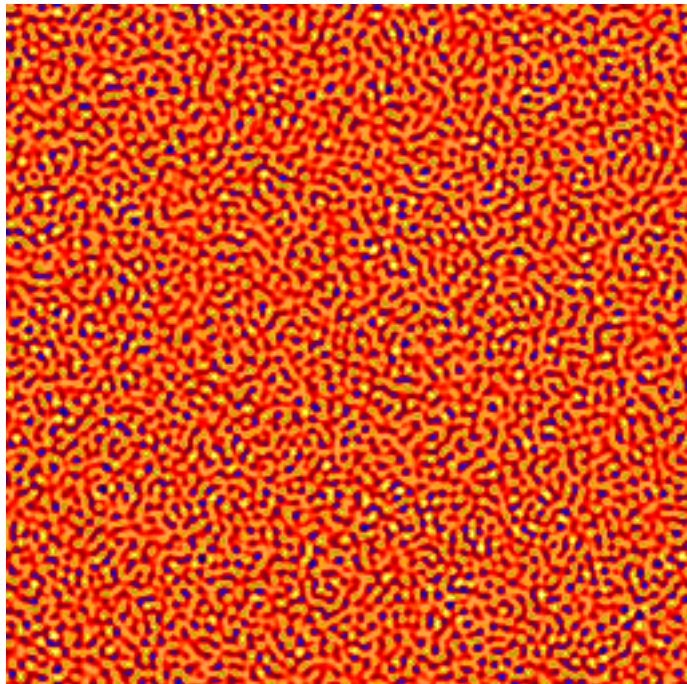
$$P = P_o \left( \frac{\rho}{\rho_o} \right)^\gamma$$

$$\rho = \rho_o \left( 1 - \frac{\gamma - 1}{\gamma} \frac{\rho_o g z}{P_o} \right)^{\frac{1}{\gamma - 1}}$$

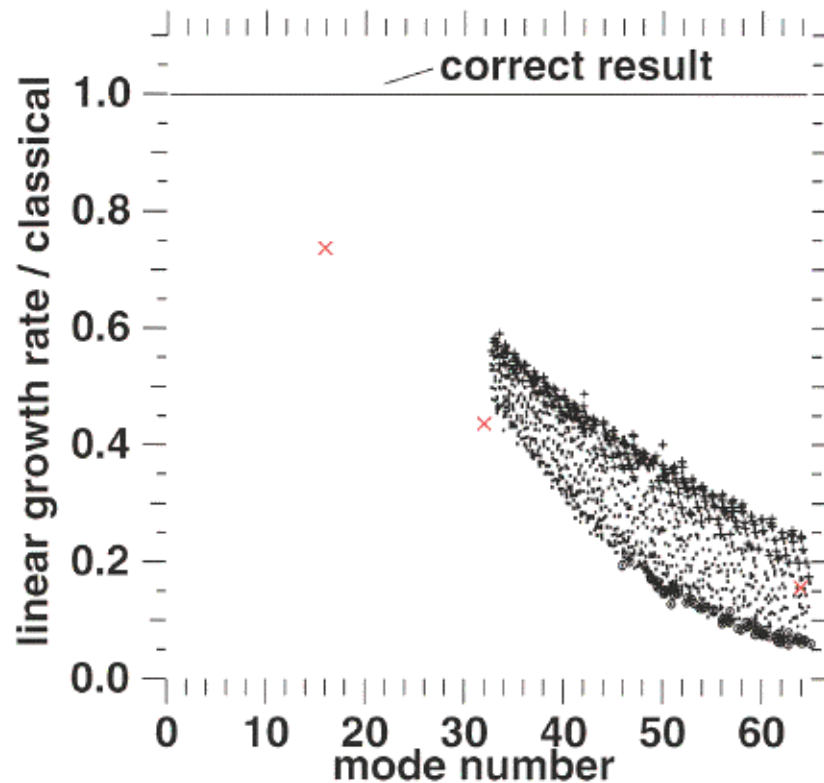
$$\gamma = 5/3, P_o = 500 \text{ dyne/cm}^2$$



Initial conditions (David Youngs) are random & distributed in wavenumber shell (**modes 32-64**) close to Nyquist limit



# Simulated linear growth rates of seed modes are far below classical due to under-resolution



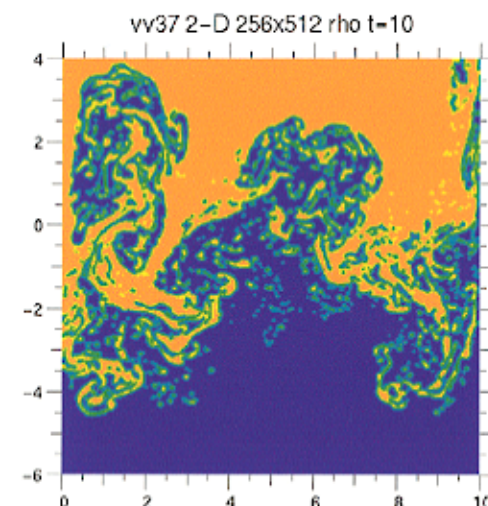
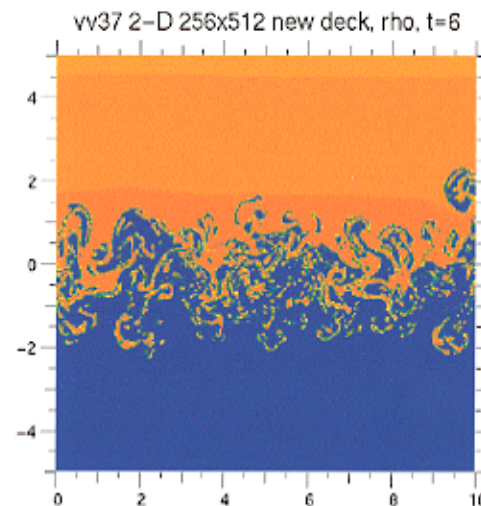
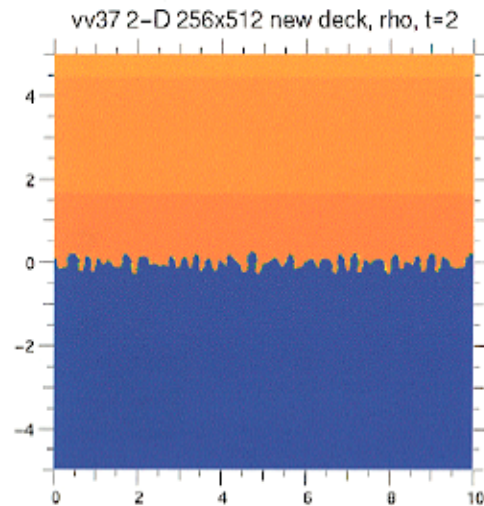
- × 2-D, single mode simulation
- + 3-D,  $k$  along mesh direction
- 3-D,  $k$  diagonal to mesh
- 3-D, all  $k$

- If the simulation were converged, all modes would grow at the classical rate
- Also note that the simulated growth rate depends upon the orientation of the wave vector,  $k$ , to the mesh

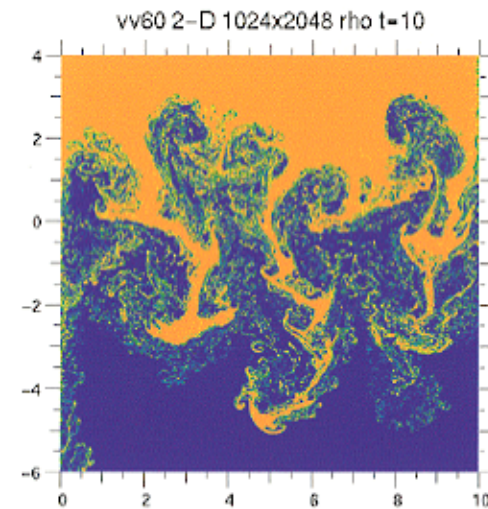
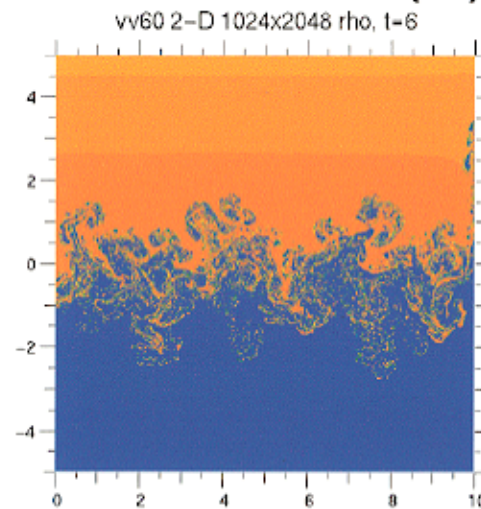
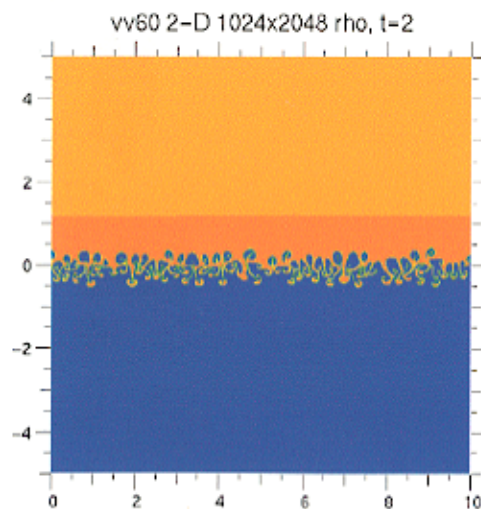
# In 2-D, the mix *extent* at late times does not change much with zoning refinement



## 2-D 256×512 (1x)

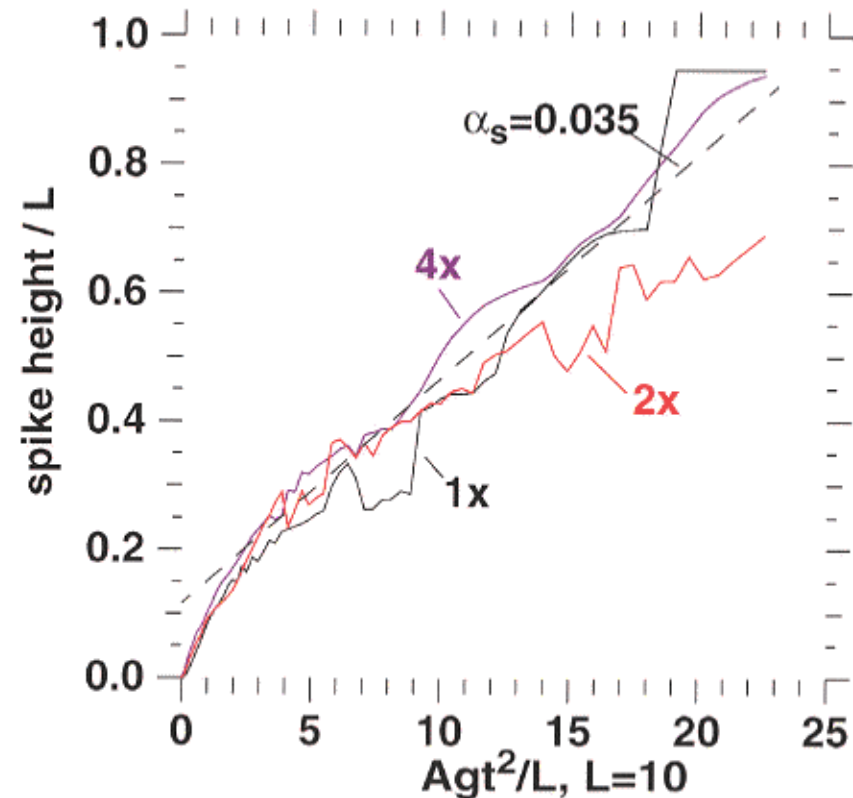
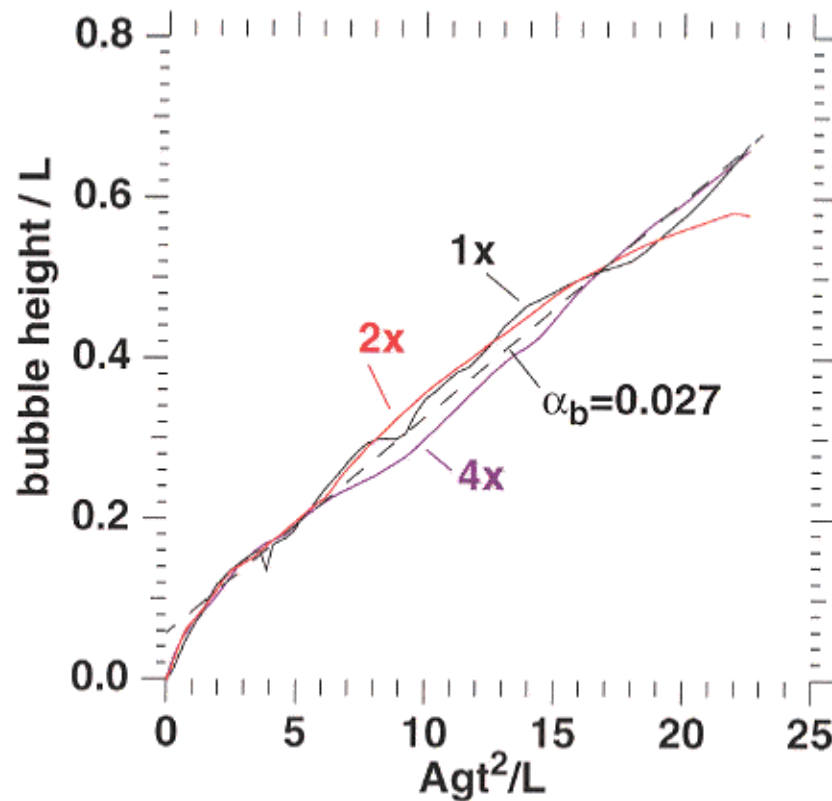


## 2-D 1024×2048 (4x)



- The seed modes are clearly under-resolved with nominal zoning

# Zoning refinement beyond the nominal resolution does not significantly affect the mix extent in 2-D runs



- 1x - nominal 256×512, 2x - 512×1024, 4x - 1024×2048
- Bubble and spike limits are taken at 1% volume fraction within  $2 < x < 8$
- The small number of large bubbles or spikes at later times introduces uncertainty due to selection statistics

# We have performed $128^2 \times 512$ 3-D simulations in one quadrant of the nominal $\alpha$ problem

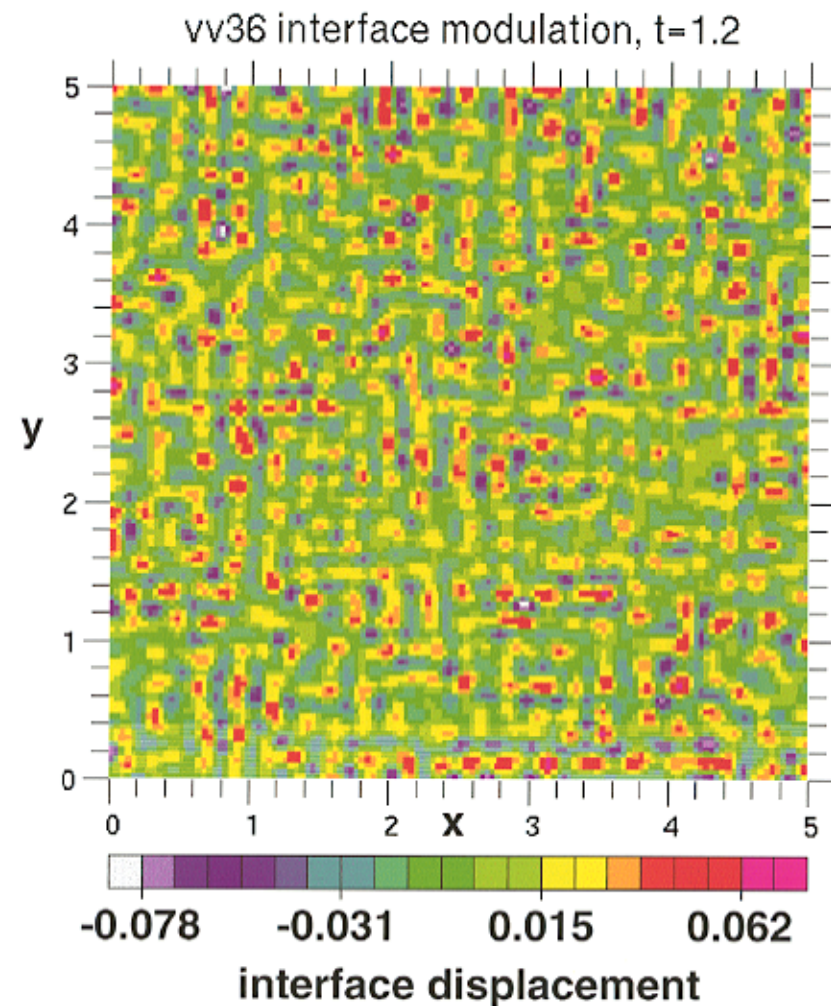
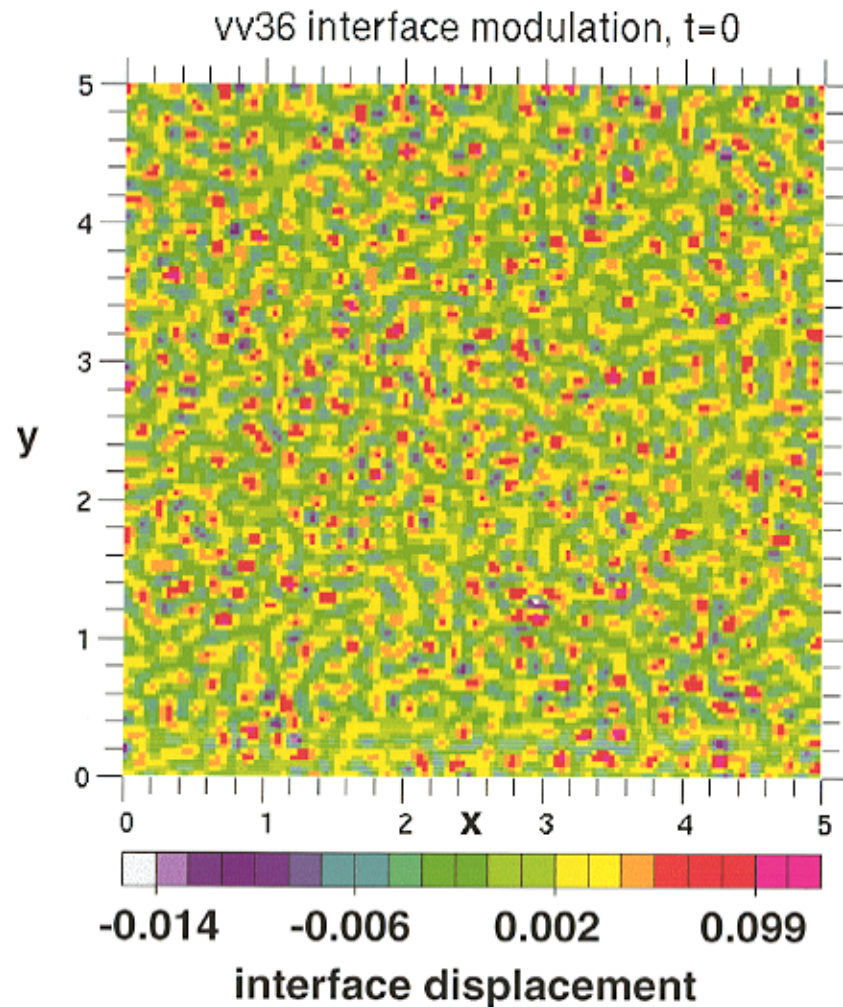
---



- We use 1/4 of the specified initial interface, a 5x5 cm square
- The zone size, initial amplitude, initial wavelengths, and  $g$  are preserved from the nominal problem (not scaled by  $L$ )
- This preserves three of the four dimensionless length ratios of the problem
  - $\lambda_0/l$
  - $a_0/l$
  - $P/(\rho g \lambda_0)$
  - $L/l$  not preserved
  - $l$  - zone size,  $a_0$  - initial amplitude,  $L$  - box size
- Results are expected to be nearly the same as for the full problem until the mix extent becomes comparable to the box width
  - This will occur earlier in time by a factor  $\sim 2^{1/2}$  than for the full problem
- We have recently completed the full size  $256^2 \times 512$  problem without interface reconstruction



# Under-resolution of the initial perturbations results in mesh imprinting - a numerical artifact



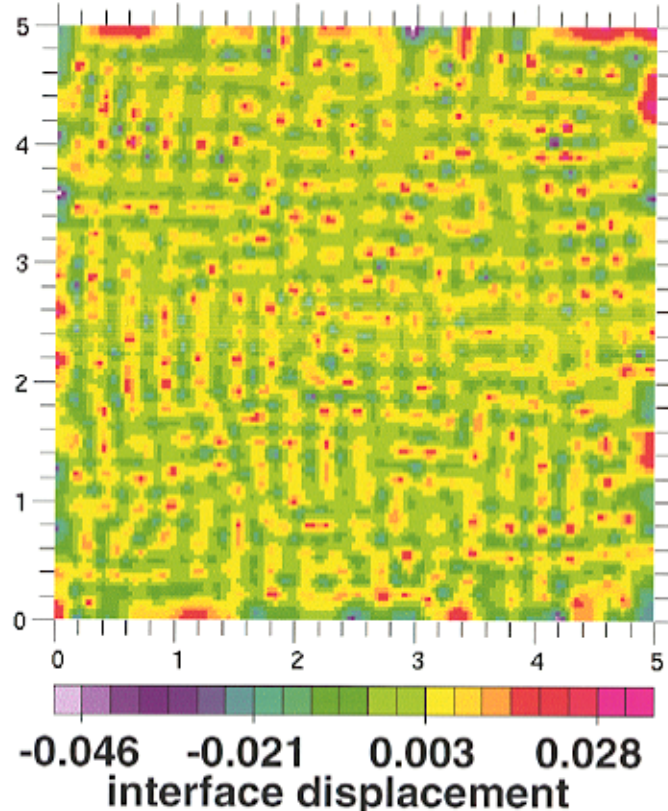
- The random isotropic initial surface evolves into a “checker board” pattern because of more rapid linear growth of modes aligned with the mesh

## The surface finish definition including sine and cosine modes should not be used with reflection boundary conditions

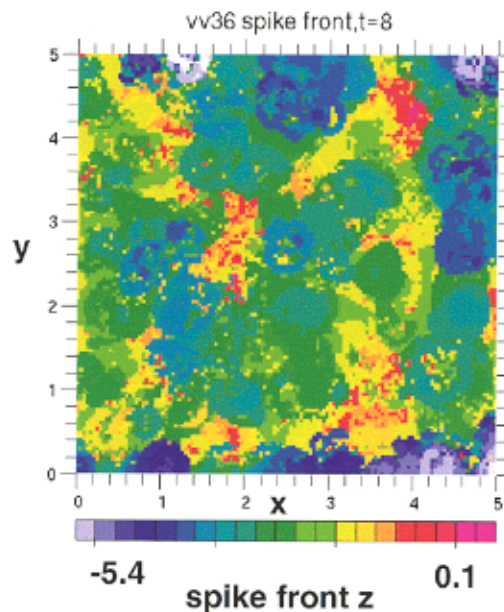
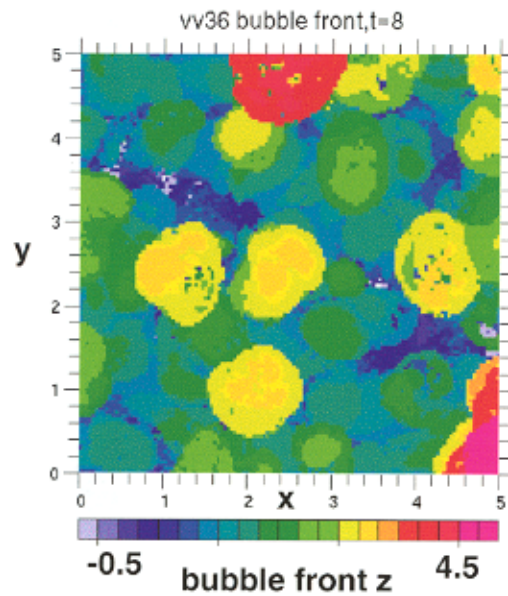


- Reflection boundary conditions support a spectrum consisting of integer and half-integer cosine modes
- Sine modes in the original surface definition are aliased into half-integer cosine modes. A “sine” mode with reflection bc has a cusp at the boundary resulting in excessive growth near the boundary even in the linear phase
- Therefore, we used a surface finish obtained from Youngs containing only cosine modes, but which looks very similar to the original surface

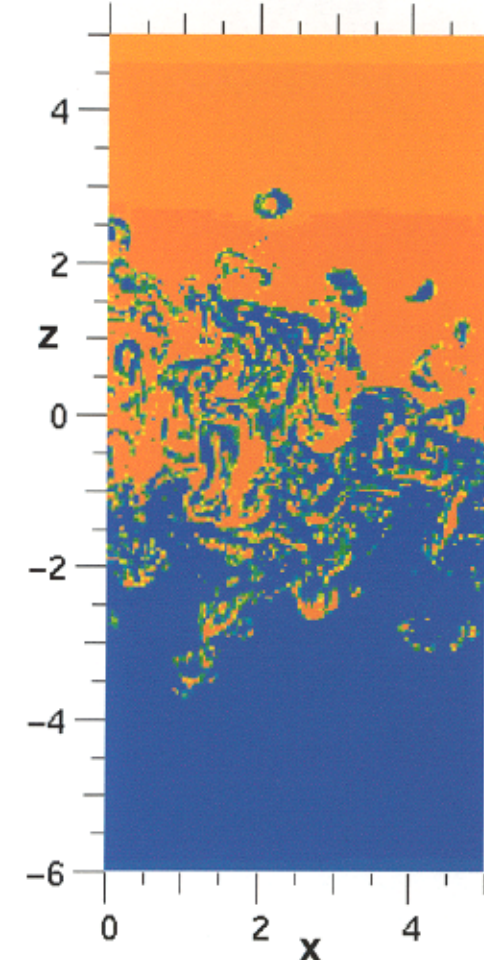
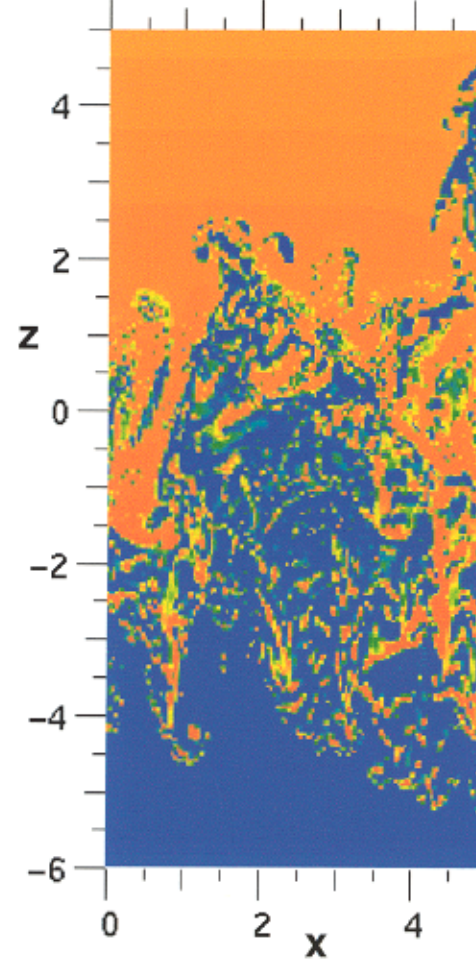
vv33 sin+cos mode, interface modulation, t=2



# Spurious enhanced penetration at faces and corners is probable a consequence of reflection boundary conditions



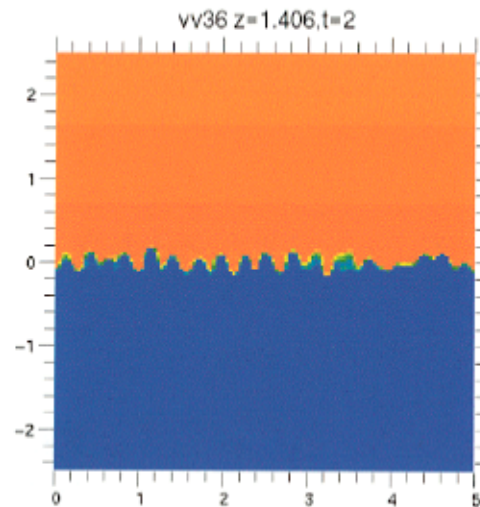
density slice, t = 8  
on face in interior



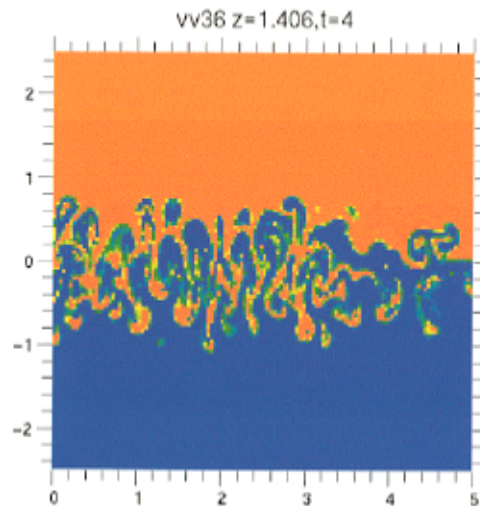
- This may result from higher symmetry of the flow at edges and corners

- Data analysis excludes volume near boundaries to minimize the influence of this effect

# The simulation with interface reconstruction shows breakup into many small drops at late times

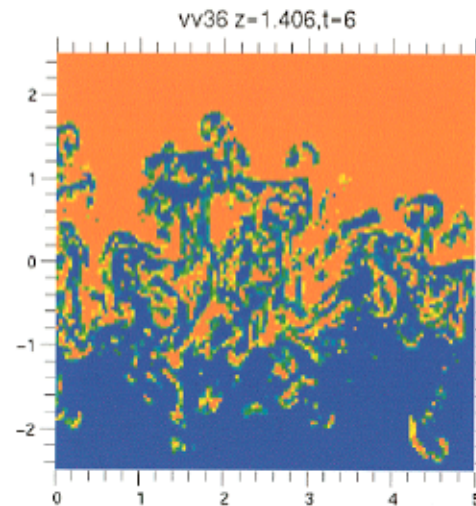


**t = 2**

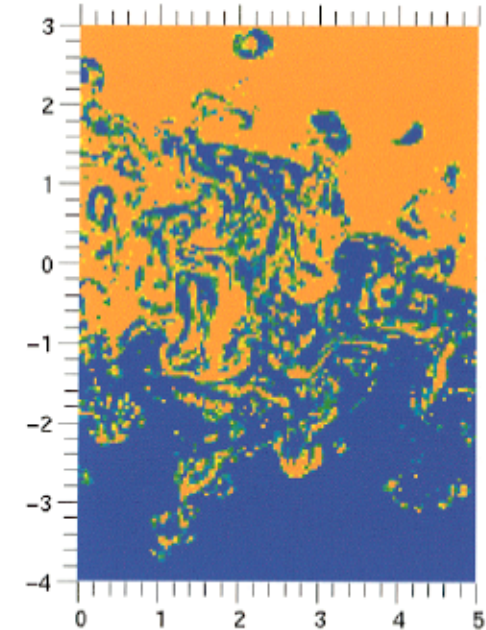


**t = 4**

- Sequence of density cuts of 3-D 1282x512 simulation in the interior (away from a face)

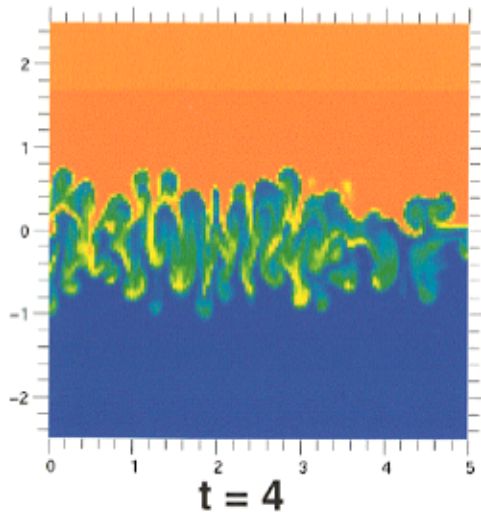
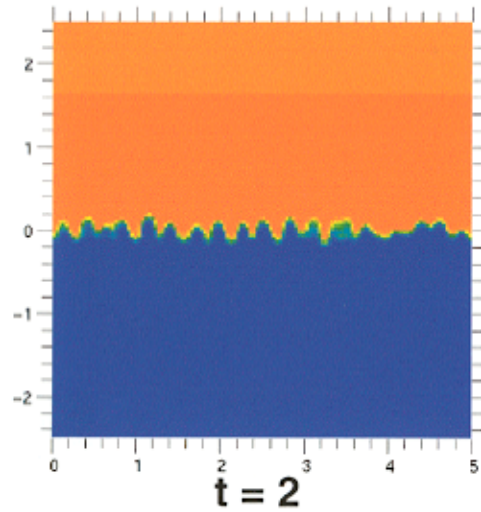


**t = 6**

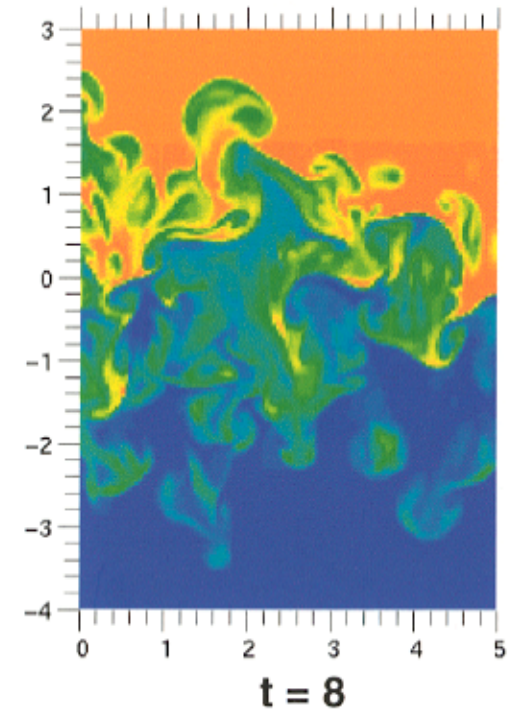
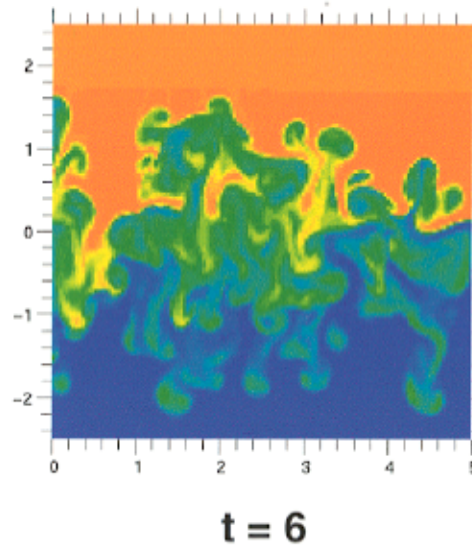


**t = 8**

# Simulations without interface reconstruction predict a mix extent only slightly lower, but show much more small scale mixing



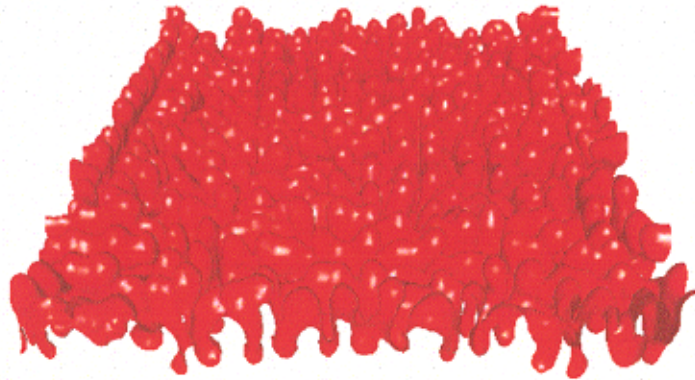
density cuts in 3-D  $128^2 \times 512$  simulation without interface reconstruction



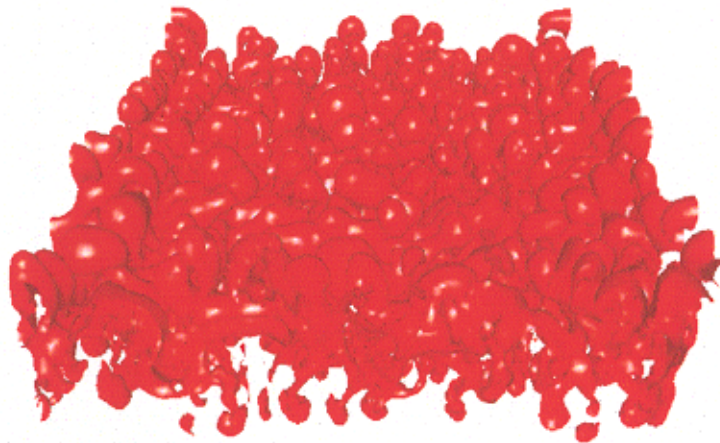
# The 3-D simulation shows the expected transition to turbulence, followed by bubble merger



visualization of interface, identified as  $\rho = 2$  contour



t = 2

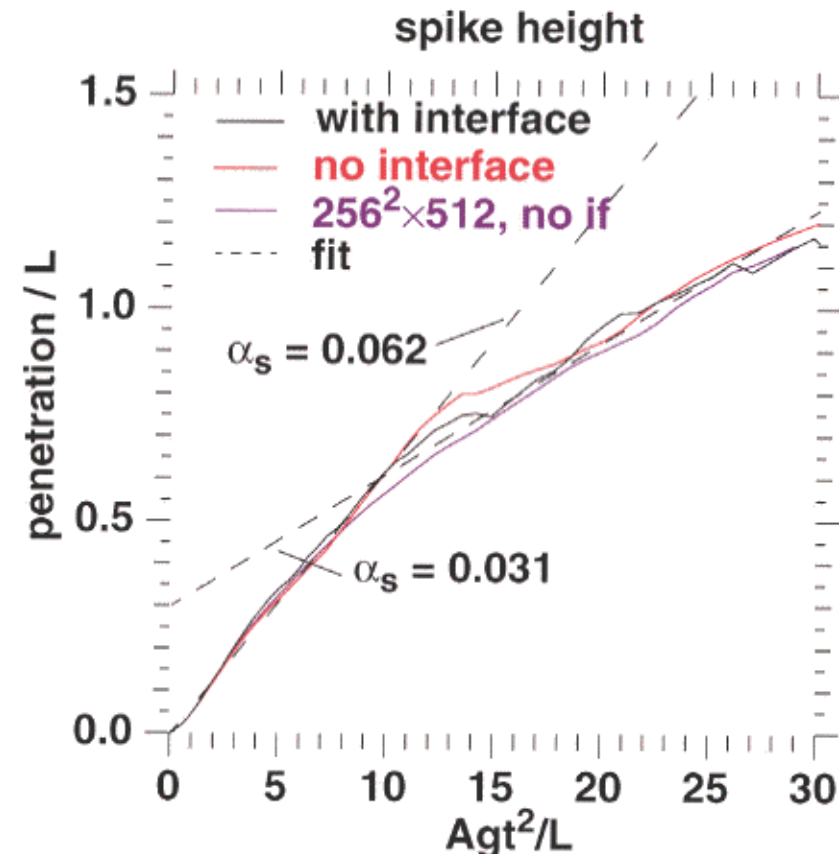
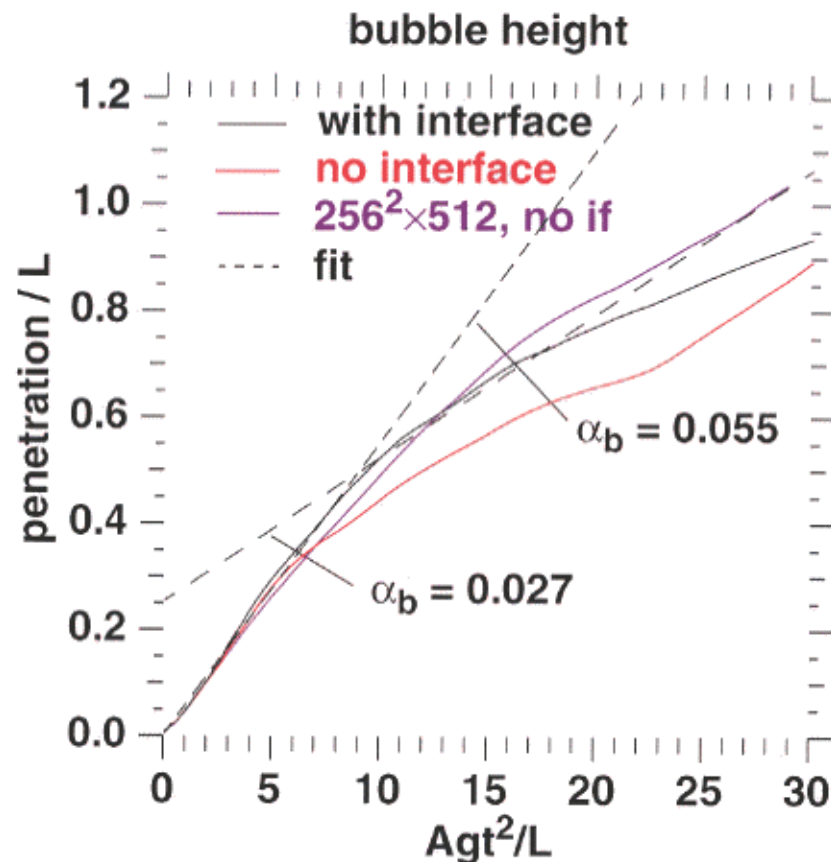


t = 4



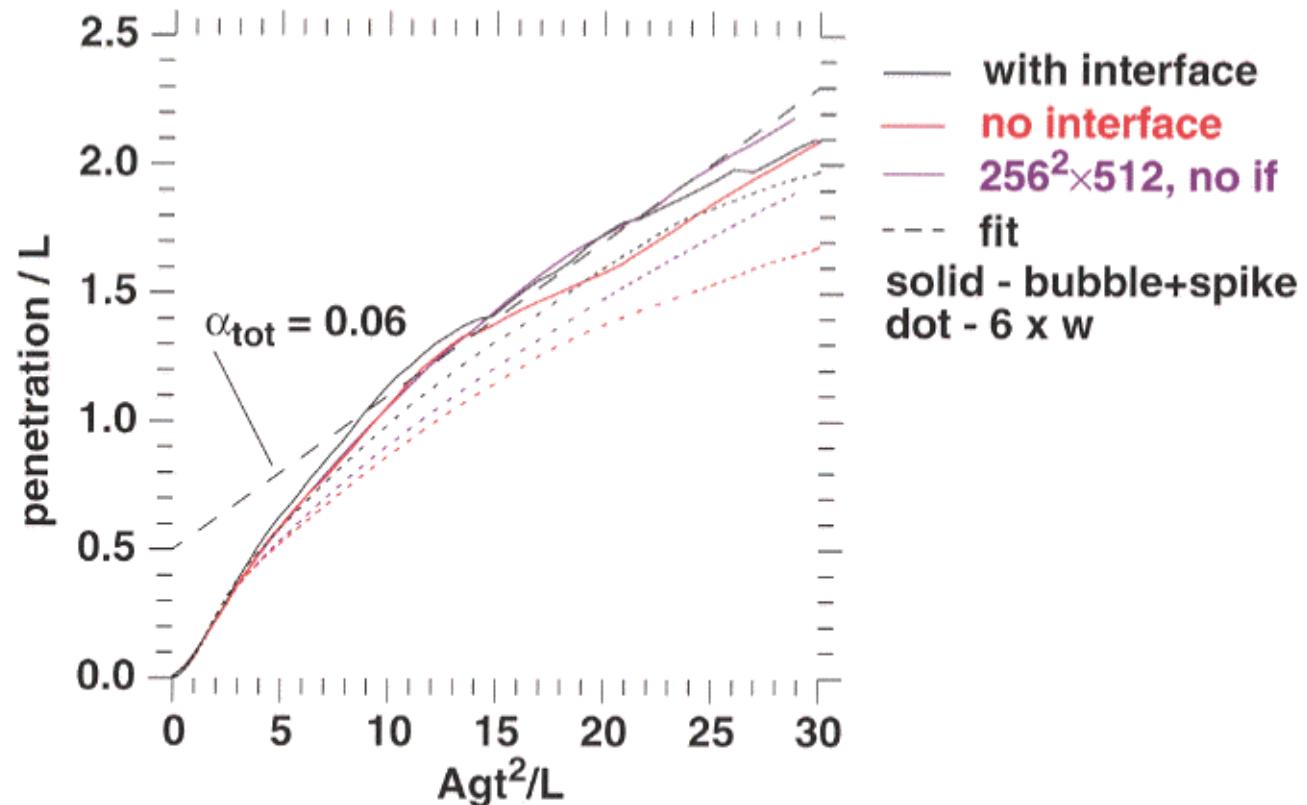
t = 6

# It is not apparent that the mix extent ever reaches an asymptotic $t^2$ growth



- “fit” lines are drawn by eye
- Interface reconstruction gives only modestly higher growth, only on the bubble side
- All cases show the slope,  $\alpha$ , decreasing with time
- On the bubble side, the full scale problem retains a higher growth rate later in time as it can grow bigger bubbles (all curves are scaled as  $L=5$ )
- The growth of the spikes does not change with problem size

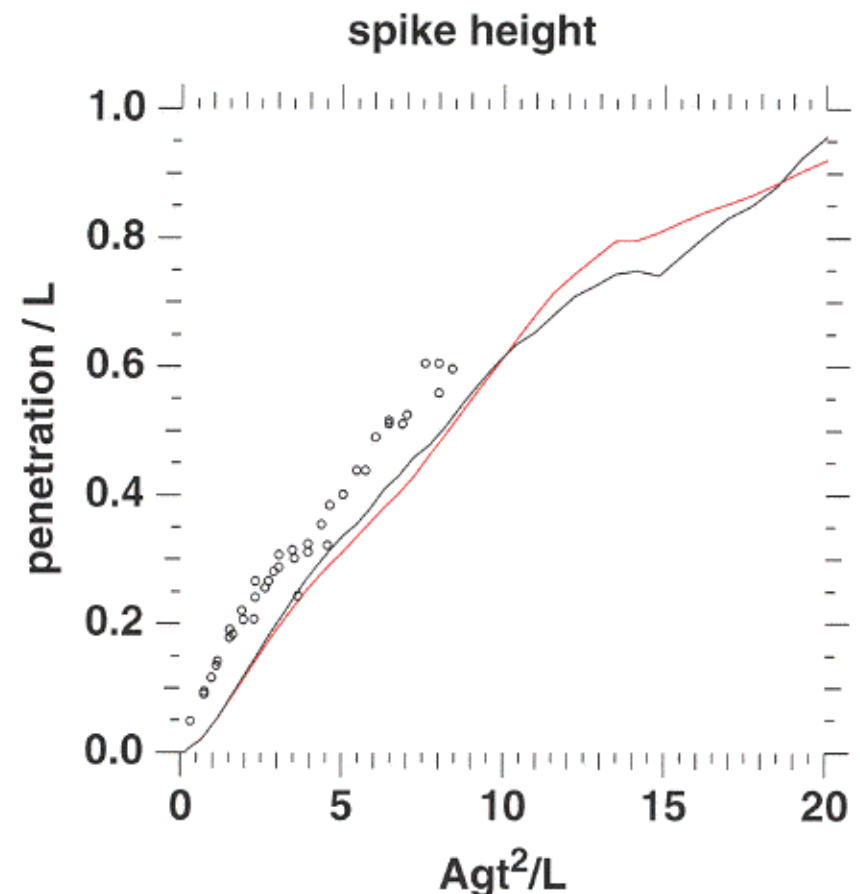
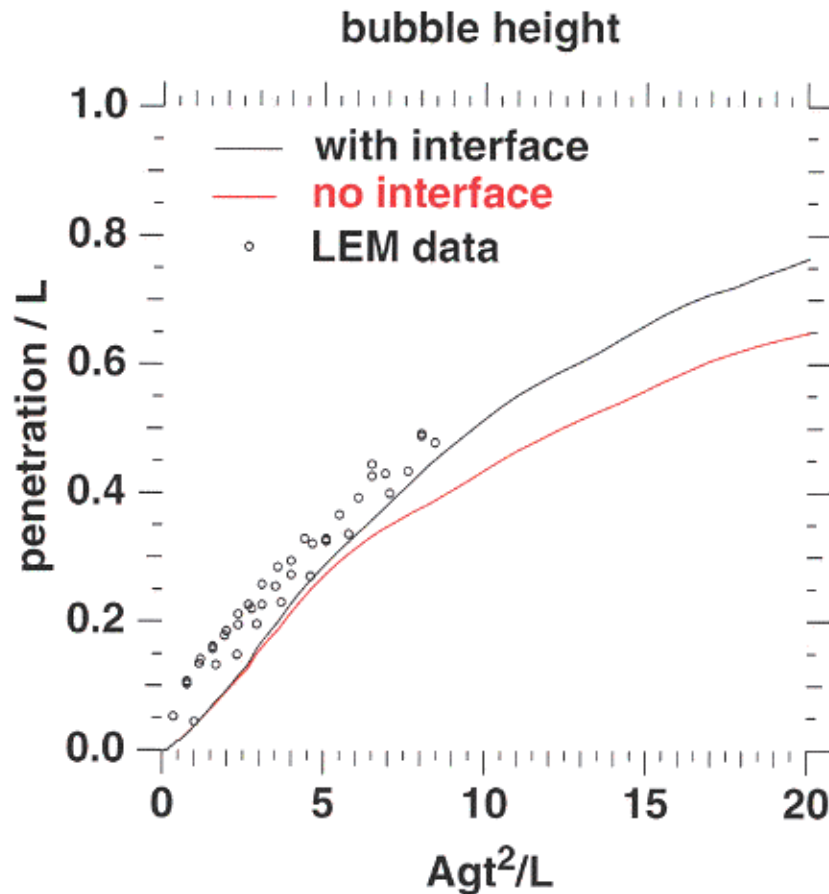
# The total mix width and integral width measure also exhibit decreasing slope with time



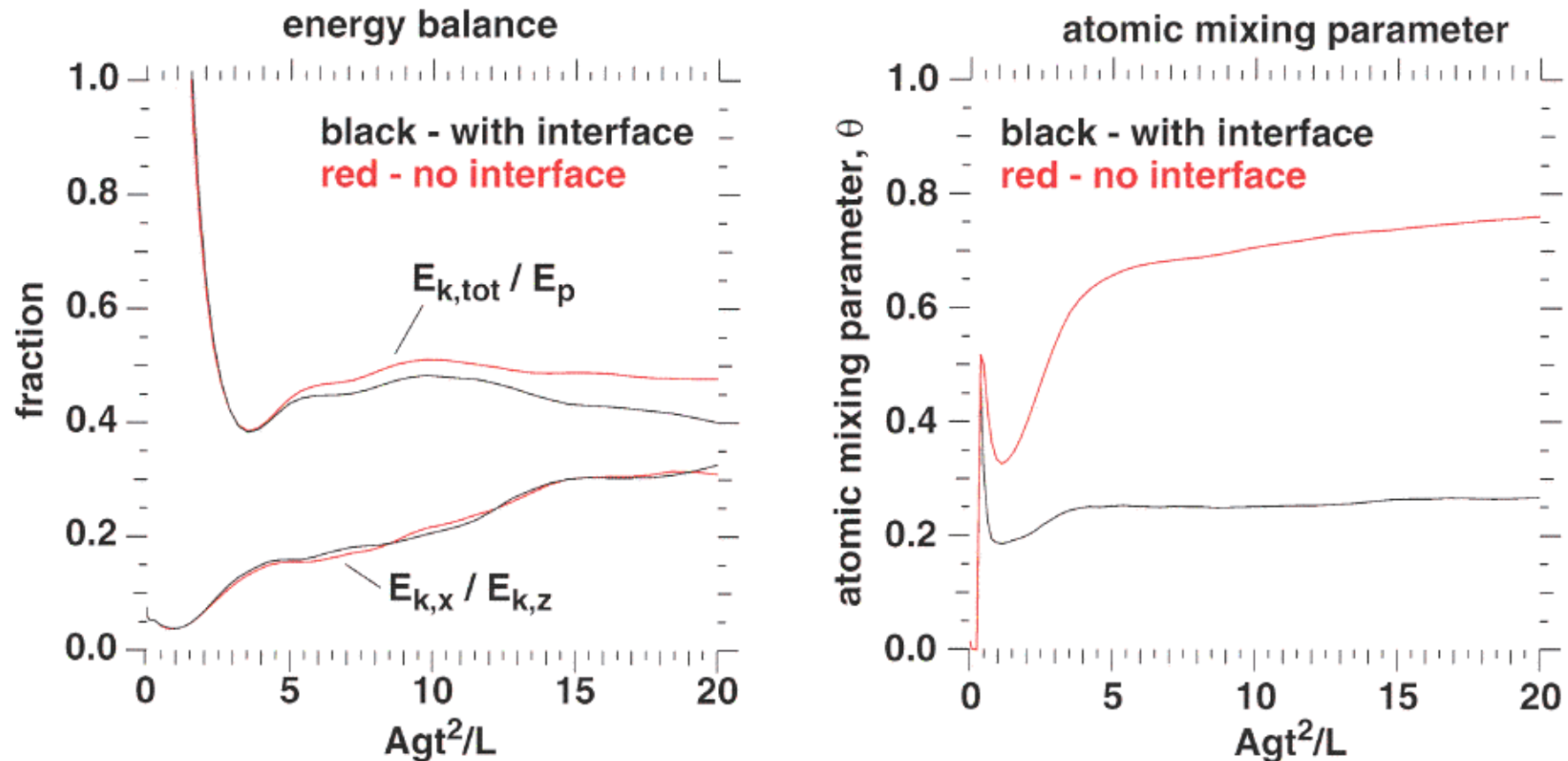
- $w$  - Andrews and Spalding integral width
- The full scale and one quadrant simulations nearly overlay when scaled with the *same*  $L$  (5 here) as the initial amplitude and wavelength were not scaled with  $L$
- We believe that the box size affects the growth only by limiting the size of the largest bubbles late in time, which is a *breakdown* of self-similarity rather than a feature of the scaling



# Simulations lie below the LEM data when scaled by the box size; however, the slope is about right

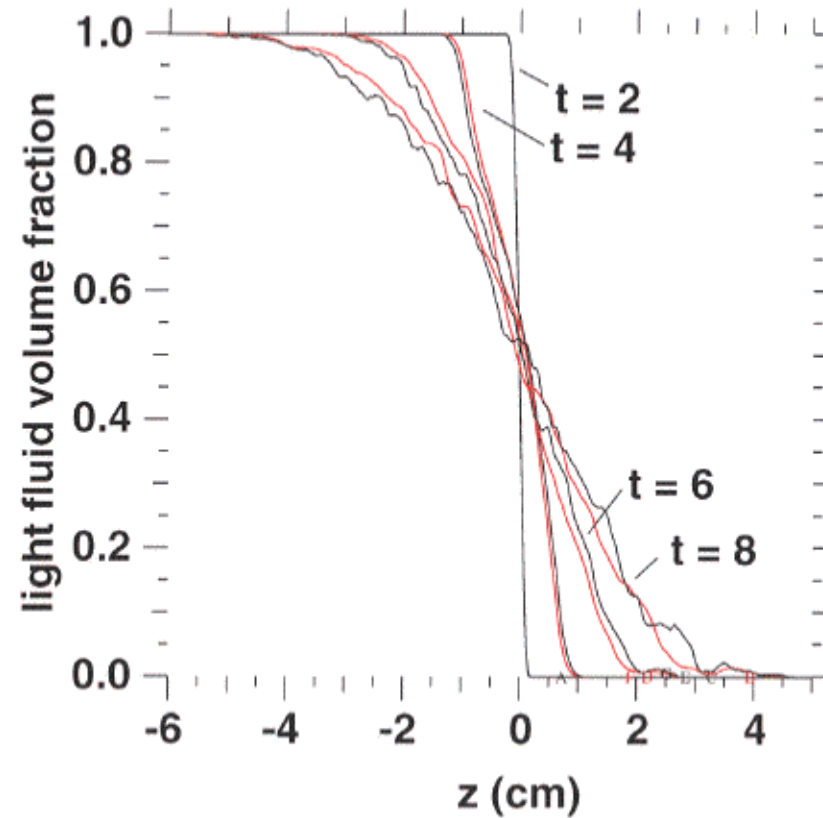


# The simulation without interface reconstruction gives atomic mixing $\sim 0.7$ , but similar dissipation to the run with tracking



- $E_p$  - potential energy drop, dissipated energy,  $E_{k,z}$  kinetic energy in streamwise direction,  $E_{k,x}$  kinetic energy in one spanwise direction,  $E_{k,tot}$  - total kinetic energy
- The atomic mixing parameter for the interface reconstruction run is an upper limit because post-processing does not account for the interface reconstruction and treats zones through which the interface passes as mixed

# Volume fraction histograms are also very similar with or without interface reconstruction



black - with interface reconstruction

red - no interface

# Conclusions

---



- Under-resolution of the initial perturbations introduces numerical artifacts, but it is uncertain if the simulated mix extent is compromised
  - 2-D runs show no significant change in mix extent with zoning refinement
- Interface reconstruction has only a modest effect on mixing extent
  - However, internal structure of the mixing zone is affected
- These runs do not appear to specify a definite value of  $\alpha$ 
  - 3-D simulations of one quadrant of the nominal  $\alpha$  problem show monotonically decreasing  $\alpha$  with increasing time
  - $\alpha_b$  drops from  $\sim 0.055$  at early times to  $\sim 0.03$  later in time
  - $\alpha_b$  remains high longer for the full scale problem
  - $\alpha_s \sim 0.06$  at early times; also appears to drop later in time
- Simulations lie below the LEM bubble, spike penetration data
  - slope of spike penetration and early time slope of bubble penetration are close to measured slopes of penetration vs.  $t^2$